

## CLAIMS

### What is claimed is:

1. A method comprising:
  - generating an isogeny that maps a plurality of points from a first elliptic curve onto a second elliptic curve;
  - publishing a public key corresponding to the isogeny;
  - encrypting a message using an encryption key corresponding to the isogeny; and
  - decrypting the encrypted message using a decryption key corresponding to the isogeny.
2. A method as recited by claim 1, wherein at least one of the encryption key or the decryption key is a private key, the private key being a dual isogeny of the isogeny.
3. A method as recited by claim 1, wherein the isogeny is generated using a technique selected from a group comprising complex multiplication generation, modular generation, linearly independent generation, and combinations thereof.

4. A method as recited by claim 1, wherein the generating maps a plurality of points from a first elliptic curve onto a plurality of elliptic curves.
5. A method as recited by claim 1, wherein the decrypting is performed by bilinear pairing.
6. A method as recited by claim 5, wherein the bilinear pairing is a pairing selected from a group comprising Weil pairing, Tate pairing, and square pairing.
7. A method as recited by claim 1, wherein the method is applied using Abelian varieties.
8. A method as recited by claim 1, wherein the method signs the message.
9. A method as recited by claim 1, wherein the method provides identity based encryption.
10. A method as recited by claim 1, further comprising composing a plurality of modular isogenies to provide the isogeny without revealing any intermediate curves.

11. A method as recited by claim 1, further comprising using a trace map down to a base field to shorten points on an elliptic curve mapped by the isogeny.
12. A method as recited by claim 1, further comprising using a trace map to shorten points on an Abelian variety.
13. A method comprising:
- publishing a public key corresponding to an isogeny that maps a plurality of points from a first elliptic curve onto a second elliptic curve;
  - and
  - decrypting an encrypted message using a decryption key corresponding to the isogeny.
14. A method as recited by claim 13, wherein the decryption key is a dual isogeny of the isogeny.
15. A method as recited by claim 13, wherein the isogeny is generated using a technique selected from a group comprising complex multiplication generation, modular generation, linearly independent generation, and combinations thereof.

16. A method as recited by claim 13, wherein the isogeny maps a plurality of points from a first elliptic curve onto a plurality of elliptic curves.
17. A method as recited by claim 13, wherein the decryption is performed by bilinear pairing.
18. A method as recited by claim 17, wherein the bilinear pairing is a pairing selected from a group comprising Weil pairing, Tate pairing, and square pairing.
19. A method as recited by claim 13, wherein the method is applied using Abelian varieties.
20. A method as recited by claim 13, wherein the method signs the message.
21. A method as recited by claim 13, wherein the method provides identity based encryption.
22. A method as recited by claim 13, further comprising using a trace map down to a base field to shorten points on an elliptic curve mapped by the isogeny.

23. A system comprising:

a first processor;

a first system memory coupled to the first processor, the first system memory storing a public key corresponding to an isogeny that maps a plurality of points from a first elliptic curve onto a second elliptic curve;

a second processor;

a second system memory coupled to the second processor, the second system memory storing an encrypted message and a decryption key corresponding to the isogeny to decrypt the encrypted message,

wherein the encrypted message is encrypted using an encryption key.

24. A system as recited by claim 23, wherein at least one of the encryption key or the decryption key is a private key, the private key being a dual isogeny of the isogeny.

25. A system as recited by claim 23, wherein the isogeny maps a plurality of points from a first elliptic curve onto a plurality of elliptic curves.

26. A system as recited by claim 23, wherein the decryption is performed by bilinear pairing.

27. A system as recited by claim 26, wherein the bilinear pairing is a pairing selected from a group comprising Weil pairing, Tate pairing, and square pairing.
28. One or more computer-readable media having instructions stored thereon that, when executed, direct a machine to perform acts comprising:
- publishing a public key corresponding to an isogeny that maps a plurality of points from a first elliptic curve onto a second elliptic curve;
  - and
  - decrypting an encrypted message using a decryption key corresponding to the isogeny.
29. One or more computer-readable media as recited by claim 28, wherein the decryption key is a private key, the private key being a dual isogeny of the isogeny.
30. One or more computer-readable media as recited by claim 28, wherein the isogeny is generated using a technique selected from a group comprising complex multiplication generation, modular generation, linearly independent generation, and combinations thereof.

31. One or more computer-readable media as recited by claim 28, wherein the isogeny maps a plurality of points from a first elliptic curve onto a plurality of elliptic curves.
32. One or more computer-readable media as recited by claim 28, wherein the decrypting is performed by bilinear pairing.
33. One or more computer-readable media as recited by claim 32, wherein the bilinear pairing is a pairing selected from a group comprising Weil pairing, Tate pairing, and square pairing.
34. One or more computer-readable media as recited by claim 28, wherein the acts are applied using Abelian varieties.
35. One or more computer-readable media as recited by claim 28, wherein the acts further comprise using a trace map down to a base field to shorten points on an elliptic curve mapped by the isogeny.
36. One or more computer-readable media as recited by claim 28, wherein the acts further comprise composing a plurality of modular isogenies to provide the isogeny without revealing any intermediate curves.

37. One or more computer-readable media as recited by claim 28, wherein the acts further comprise using a trace map to shorten points on an Abelian variety.

38. One or more computer-readable media as recited by claim 28, wherein the acts sign the message.

39. One or more computer-readable media as recited by claim 28, wherein the acts provide identity based encryption.